2.7 Composite functions

2.7.1 Graph the composition of two functions

Suppose you want graph $(f \circ g)(x)$ for the following functions:

$$f(x) = x^2 - 2x + 5,$$
 $g(x) = \frac{x+3}{4}.$

- ① Create a new document, press and select Add Calculator.
- ② Enter the two expressions f(x) and g(x), each in a different line. To do this, write ' $\mathbf{f}(\mathbf{x})$ ' and press **ctrl** then **i**. Then, write the expression function of x. Do the same for g(x).
- 3 Write f(g(x)) in a third line and press enter. The result is displayed:

∢ 1.1 ▶	*Doc	CAPS RAD 📘 🗙
$f(x):=x^2-2 \cdot x+5$		Done
$g(x) := \frac{x+3}{4}$		Done
<i>f</i> (g(x))		$\frac{x^2}{16} - \frac{x}{8} + \frac{65}{16}$

- To plot the function, open a new page by pressing **t** then **b**. Select Add Graphs.
- **5** Write f1(x) = f(g(x))' and press enter .
- Choose an appropriate window. To do that, press and select Window /Zoom > Window Settings. Enter the appropriate values of Xmin, Xmax, Ymin and Ymax. The following graph should be displayed (with Xmin=-30, Xmax=30, Ymin=-100, Ymax=100):



2.7.2 Compute specific value of the composition of two functions

Suppose you want to evaluate $(f \circ g)(1)$ for the following functions:

$$f(x) = x^2 - 2x + 5 \qquad \qquad g(x) = \frac{x+3}{4}.$$

① Create a new document, press and select Add Calculator.

② Enter the two expressions f(x) and g(x), each in a different line. To do this, write $\mathbf{f}(\mathbf{x})'$ and press \mathbf{ctrl} then \mathbf{free} . Then, write the expression function of x. Do the same for g(x).

3 Write f(g(1))' in a third line and press $\overline{e_{nter}}$. The result is displayed:

◀ 1.1 1.2 1.3 ▶	*Doc	CAPS RAD	×
$f(x):=x^2-2 \cdot x+5$		Done	•
$g(x) := \frac{x+3}{4}$		Done	
f(g(1))		4	
I			

The result should be 4. Thus $(f \circ g)(1) = 4$.

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